Friendly Corecursion in

Jasmin Blanchette, Aymeric Bouzy, Andreas Lochbihler,
Andrei Popescu, Dmitriy Traytel

Context

Proof assistants = Tools for

      Defining mathematical concepts

      Proving facts about them

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What makes a good proof assistant?

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$$f : \mathsf{Nat} \rightarrow \mathsf{LazyList}(\mathsf{Nat})$$

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$$\mathsf{f}: \; \mathsf{Nat} \; \rightarrow \; \mathsf{LazyList}\,(\mathsf{Nat})$$

$$\mathsf{f}(n) = \begin{cases} [] & \text{if } n \leq 1 \\ \mathsf{f}(n\,/\,2) & \text{if } n > 1 \text{ and } n \text{ even} \\ n \; \#\# \; \mathsf{f}(3 * n + 1) & \text{if } n > 1 \text{ and } n \text{ odd} \end{cases}$$

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